

Fuzzy Soft set Operations and Priority Decision Making with Fuzzy soft Set Relation Operator

Dr. Rajesh Kumar Pal

*Associate professor, Dept. of Mathematics,
DAV(PG) college, Dehradun (U.K.)-248001, India.*

ABSTRACT

Generally in our day to day life we come across the real life situations when right decision making becomes difficult. In different fields like economics, social science, medical science, environment, where such complicity arises and involves uncertainties. The conventional mathematical methods are unsuitable to solve such problems. To solve this problem, we are to find the various parameters related to the problem to use them to get the accurate result. So fuzzy soft set theory is the best mathematical tool for solving such problems using different techniques. In this research paper, we have defined some fundamental definitions and fuzzy soft operations along with a specific fuzzy soft operator i.e. Fuzzy soft relation operator with application in real life decision making problem.

Keywords: Fuzzy set; fuzzy soft set; fuzzy soft relation operator.

1. INTRODUCTION

In the fields of engineering, economics, social science, medical science, environment, etc. many complicated problems arise “involving uncertainties, classical methods are found to be inadequate in recent times”. To deal with this uncertainty, in 1965 Zadeh [1] developed the theory of fuzzy sets. Molodtsov [2] pointed out that existing theories, namely Probability Theory, Intuitionistic Fuzzy Set Theory, Fuzzy Set Theory, Rough Set Theory etc. have their own limitations for solving problems regarding uncertainties. He also explained that there are some limitation for solution due to the inadequacy of the parameterization tool of the fuzzy set theory, as such problems have multi-criteria in objects. He initiated the novel concept of Soft Set in 1999 as a new mathematical tool to deal with this problem. This soft set theory can be

merged with previous theories. Scholars have proposed Probabilistic soft sets (Fatimah et al. [3]), Fuzzy soft sets (Maji et al. [4]), etc. In this paper, we are defining fuzzy set, fuzzy soft set and operations on soft sets and fuzzy soft sets. We have taken a specific fuzzy soft set relation operator defined by Kalaichelavi et al. [28] and applied this operation for priority decision making in real life problem.

2. MATHEMATICAL BACKGROUND

This new soft set theory found to be very useful in different fields using different techniques and showed great success. Molodtsov [2,5,6,7] applied this theory with different techniques formulating as the notions of soft number, soft integral and soft derivative etc. Maji et al. [8,9] studied it in detail and applied in decision making problems. Pawlak [10] proposed the reduction of rough sets, while Kong et al. [11] presented the normal parameterization reduction of soft sets and Chen et al. [12] gave parameterization reduction of soft sets. Zhan et al. [13] did a comprehensive study of that problem.

To obtain a better result in a more justified manner, many researchers used parameters through a different mathematical approach. Xiao et al. [14] formulated synthetic evaluation method, and gave a recognition for soft information based on the theory of soft sets [15]. Mushrif et al. [16] developed the algorithm based on the notions of soft set theory. Pei and Miao [17] worked on the soft sets to show a class of special information system, while Zou and Xiao [18] presented data analysis approaches of soft sets. Kovkov DV et al. [19] worked on optimization problems, whereas Majumdar and Samanta [20] worked on the similarity of soft sets and Ali et al. [21] presented a few new operations in soft set theory.

Many scholars around the globe presented their work with different novel concepts in interesting way to obtain more accurate result. Maji et al. [4] presented the concept of fuzzy soft sets by embedding the idea of fuzzy sets, whereas Roy and Maji [22] presented a different application of fs sets. Som [23] defined fuzzy soft relations and soft set relations. Krishna G et al. [24] worked on fuzzy soft set and Bhardwaj et al. [25] used Reduct soft set for real life decision making problems. Alcantud et al. [26] presented a concept of Partial Valuation Fuzzy Soft Set (PVFSS) and introduced the application of data filling in PVFSS. Irkin [27] generated the sensory score and presented a fuzzy soft set modeling in his study to find the maximum score. Kalaichelavi et al. [28], Karaca and Tas [29] presented notions of soft set and fuzzy soft sets. Ozgur and Tas [30] introduce a new method to include the notion of period using soft set and matrix form theories for solving investment decision making problem. Tas et al. [31] applied soft set theory and fuzzy soft set theory for the effective measurement of stock-out situations.

Maji et al. [4,9] defined the fundamental definitions of soft sets and fs sets which are used as an important basic operation. But Chen D, et al. [12], Pei and Miao [17], Kong et al. [32] and Ali et al. [21] pointed out some weak points of earlier work. Cogman and Enginoglu [33] redefined the operations of soft sets to develop the

theory which became more functional for improving the approach and results. Cogman and Enginoglu [34] later came up with a soft matrix theory. Cagman et al. [35] defined a fuzzy parameterized soft set theory and its application.

3. BASIC DEFINITIONS[37].:

In this section, we present the basic definitions of fuzzy set theory [1] and soft set theory [2] that are useful for subsequent discussions. Throughout this work, U refers to an initial universe, E is a set of parameters, $P(U)$ is the power set of U , and $A \subseteq E$.

Let us recall the notation of Fuzzy Set as follows:

3.1. Fuzzy Set: A fuzzy set X over a universal set U is a set defined by a function μ_X performing a mapping

$$\mu_X : U \rightarrow [0, 1]$$

here, this μ_X is the membership function of X , and the value $\mu_X(u)$ will be the grade of membership of $u \in U$. The value shows the degree of u belongingness to the fuzzy set X . So, a fuzzy set X over U can be defined as follows:

$$X = \{(\mu_X(u)/u), u \in U, \mu_X(u) \in [0, 1]\}.$$

The set of all the fuzzy sets over U will be denoted by $F(U)$.

3.2 Soft set: Let X be a universe of discourse, E be set of parameters and $A \subseteq E$, then (F, A) is called a soft set over X , where F is a mapping given by $F: A \rightarrow P(X)$, $P(X)$ is the power set of X , i.e. for $e \in A$ represents the set of all e -approximate members of the soft set (F, A) .

for example Let $X = \{p_1, p_2, p_3\}$ be the set of three products and $E = \{e_1(\text{good looking}), e_2(\text{cheaper}), e_3(\text{Durable})\}$ be the set of parameters and $A = \{e_1, e_3\} \subset E$ then $(F, A) = \{F(e_1) = \{p_1, p_2\}, F(e_3) = \{p_1, p_3\}\}$ is a soft set over X .

A soft set F_A over U is a set defined by a function f_A representing a mapping

$$f_A : E \rightarrow P(U) \text{ such that } f_A(x) = \emptyset ; \text{ if } x \notin A$$

Here, f_A is called approximate function of the soft set F_A , and the value $f_A(x)$ is a set called x -element of the soft set for all $x \in E$. The sets $f_A(x)$ may be empty, arbitrary or have nonempty intersection. So a soft set $[F, A]$ $F_A = \{(x, f_A(x)) : x \in E, f_A(x) \in P(U)\}$ over a universal set U can be shown as the set of ordered pairs such that

$$F_A = \{(x, F_A(x)) : x \in E, F_A(x) \in P(U)\}$$

the set $S(U)$ is the set of all soft sets over U .

Example: Let $U = \{u_1, u_2, u_3, u_4, u_5\}$ be a universal set and $E = \{x_1, x_2, x_3, x_4\}$ be a set of parameters. If $A = \{x_1, x_2, x_4\} \subseteq E$, $f_A(x_1) = \{u_2, u_4\}$, $f_A(x_2) = U$ and $f_A(x_4) = \{u_1, u_3, u_5\}$, this soft set F_A is written by

$$F_A = \{(x_1, \{u_2, u_4\}), (x_2, U), (x_4, \{u_1, u_3, u_5\})\}.$$

In the soft sets, the approximate functions and the parameter sets are crisp. But in the fs-sets, while the parameters sets are crisp, the approximate functions are fuzzy subsets of U . From now on, we will use $\Gamma_A, \Gamma_B, \Gamma_C, \dots$, etc. for fs-sets and $\gamma_A, \gamma_B, \gamma_C$, etc. for their fuzzy approximate functions, respectively.

3.3 Fuzzy Soft Set: Let X be a universal set, E be set of parameters and $A \subseteq E$. We can represent the pair (F, A) as fuzzy soft set over X where F is a mapping given by $F: A \rightarrow I^X$, Where I^X denote the set of all fuzzy subsets of X .

for example Let $X = \{p_1, p_2, p_3\}$ be the set of three products and $E = \{e_1(\text{good looking}), e_2(\text{cheaper}), e_3(\text{Durable})\}$ be the set of parameters and $A = \{e_1, e_3\} \subset E$ then $(F, A) = \{F(e_1) = \{(p_1, 0.3), (p_2, 0.5)\}, F(e_3) = \{(p_1, 0.3), (p_3, 0.7)\}\}$ is a fuzzy soft set over X .

or fs Set: An fs-set Γ_A over U is a set defined by a function γ_A representing a function $\gamma_A: E \rightarrow F(U)$ such that $\gamma_A(x) = \emptyset$; if $x \notin A$:

Here, γ_A is called fuzzy approximate function of the fs-set Γ_A , and the value $\gamma_A(x)$ is a set called x -element of the fs-set for all $x \in E$. Thus, an fs-set Γ_A over U can be represented by the set of ordered pairs

$$\Gamma_A = \{(x, \gamma_A(x)) : x \in E; \gamma_A(x) \in F(U)\}:$$

Note that the set of all fs-sets over U will be denoted by $FS(U)$.

Example. Let $U = \{u_1, u_2, u_3, u_4, u_5\}$ be a universal set and $E = \{x_1, x_2, x_3, x_4\}$ be a set of parameters. If $A = \{x_1, x_2, x_4\}$ and $A \subseteq E$, $\gamma_A(x_1) = \{0.8/u_2, 0.4/u_4\}$, $\gamma_A(x_2) = U$, and $\gamma_A(x_4) = \{0.3/u_1, 0.5/u_3, 0.7/u_5\}$ then the soft set F_A is written by

$$F_A = \{(x_1, \{0.8/u_2, 0.4/u_4\}), (x_2; U), (x_4, \{0.3/u_1, 0.5/u_3, 0.7/u_5\})\}.$$

3.4. Empty fs-set: Let $\Gamma_A \in FS(U)$. If $\gamma_A(x) = \emptyset$; for all $x \in E$, then Γ_A is called an empty fs-set, denoted by $\Gamma\Phi$.

3.5. Universal fs-set: Suppose $\Gamma_A \in FS(U)$ and If $\gamma_A(x) = U$ for all $x \in A$, then Γ_A is called A -universal fs-set. If $A = E$, then the A -universal fs-set is called universal fs-set, denoted by $\Gamma\bar{E}$.

Example. Assume that $U = \{u_1, u_2, u_3, u_4, u_5\}$ is a universal set and $E = \{x_1, x_2, x_3, x_4\}$ is a set of all parameters.

If $A = \{x_2, x_3, x_4\}$, $\gamma_A(x_2) = \{0.4/u_2, 0.8/u_4\}$, $\gamma_A(x_3) = \emptyset$; and $\gamma_A(x_4) = U$, then the fs-set Γ_A is written by $\Gamma_A = \{(x_2, \{0.4/u_2, 0.8/u_4\}), (x_4, U)\}$.

If $B = \{x_1, x_3\}$, and $\gamma_B(x_1) = \emptyset$, $\gamma_B(x_3) = \emptyset$, then the fs-set Γ_B is an empty fs-set, i.e. $\Gamma_B = \Gamma_\emptyset$.

If $C = \{x_1, x_2\}$, $\gamma_C(x_1) = U$, and $\gamma_C(x_2) = U$, then the fs-set Γ_C is a C-universal fs-set, i.e., $\Gamma_C = \Gamma_{C^{\sim}}$.

If $D = E$, and $\gamma_D(x_i) = U$ for all $x_i \in E$, where $i = 1, 2, 3, 4$, then the fs-set Γ_D is a universal fs-set, i.e., $\Gamma_D = \Gamma_{\tilde{E}}$.

4. OPERATIONS ON SOFT SETS AND FUZZY SOFT SETS [36]:

Let (F,A) and (G,B) be two soft set over common universe X where $A, B \subseteq E$, then

- (i) (F,A) is a sub soft set of (G,B) written as $(F,A) \subseteq (G,B)$ if $A \subseteq B$ and $F(e) \subseteq G(e)$, $\forall e \in A$
- (ii) $(F,A) = (G,B)$ if $(F,A) \subseteq (G,B)$ and $(G,B) \subseteq (F,A)$
- (iii) The compliment of a soft set (F,A) denoted by $(F,A)^c = (F^c, A)$, where $F^c: A \rightarrow 2^X$ such that $F^c(e) = X - F(e)$, $\forall e \in A$
- (iv) A soft set (F,A) is said to be a null soft set if $\forall e \in A$, $F(e) = \emptyset$ where \emptyset is the null set of X .
- (v) AND operation of two soft sets
 “ (F,A) AND $((G,B))$ ” denoted by $(H, A \times B) = (F,A) \wedge (G,B)$, is defined as $H(\alpha, \beta) = F(\alpha) \cap G(\beta)$, $\forall (\alpha, \beta) \in A \times B$
- (vi) OR operation of two soft sets
 “ (F,A) OR $((G,B))$ ” denoted by $(O, A \times B) = (F,A) \vee (G,B)$, is defined as $O(\alpha, \beta) = F(\alpha) \cup G(\beta)$, $\forall (\alpha, \beta) \in A \times B$.
- (vii) Intersection of two soft sets (F,A) and (G,B) over the common universe X is the soft set $(I,C) = (F,A) \cap (G,B)$, where $C = A \cap B$ and $I: C \rightarrow 2^X$ such that $I(e) = F(e) \cap G(e)$, $\forall e \in C$
- (viii) Union of two soft sets (F,A) and (G,B) over the common universe X is the soft set $(U,C) = (F,A) \cup (G,B)$, where $C = A \cup B$ and $U: C \rightarrow 2^X$ such that $\forall e \in C$

$$U(e) = \begin{cases} F(e), & e \in A \sim B \\ G(e), & e \in B \sim A \\ F(e) \cup G(e), & e \in A \cap B \end{cases}$$

The definitions of sub fuzzy soft set, null fuzzy soft set and operations of intersection, union for fuzzy soft set are similar to those defined for soft sets.

5. PROPOSITION ON SOFT SETS (OR FUZZY SOFT SETS)[36]:

If (F,A) and (G,B) are two soft sets (or fuzzy soft sets) then

- (i) $(F,A) \cup (F,A) = (F,A)$
- (ii) $(F,A) \cap (F,A) = (F,A)$
- (iii) $(F,A) \cup \phi = \phi$
- (iv) $(F,A) \cap \phi = \phi$
- (v) $\{(F,A) \cup (G,B)\}^C = (F,A)^C \cup (G,B)^C$
- (vi) $\{(F,A) \cap (G,B)\}^C = (F,A)^C \cap (G,B)^C$

6. DECISION MAKING IN REAL LIFE PROBLEM:**(A) Fuzzy soft Set Relation Operator**

Let (F, A) and (G, B) be two fuzzy soft sets over a common Universal set. Then a relation R of (F, A) on (G, B) may be defined as a mapping $R: AXB \rightarrow P(U^2)$ such that for each $e_i \in A$, $e_j \in B$ for all $\mu_i \in F(e_i)$, $\mu_k \in G(e_j)$.

The relation R is characterized by the following membership function

$$\mu_R(\mu_i, \mu_k) = \mu_F(e_i)(u_i) \times \mu_G(e_j)(\mu_k), \text{ where } u_i \in F(e_i), u_k \in G(e_j)$$

(B) Application:

A company wants to establish his new office in a state. The company gave the demand for the survey data based on various parameters of the cities in the state to the three different agencies viz. A_1, A_2, A_3 . The set of alternatives of four cities in the state is $U = \{c_1, c_2, c_3, c_4\}$. The various parameters of the study of these cities are population of the city, distance from Airport & Railway Station, Available skilled man power in the city, Distance from the capital of the state and Crime rate in the city. They give different weights to the parameters in terms of fuzzy set to each city. Thus the set of parameters is $E = \{x_1, x_2, x_3, x_4, x_5\}$

where

$x_1 =$ Population of the city

$x_2 =$ Distance from Airport & Railway Station

$x_3 =$, Available skilled man power in the city

$x_4 =$, Distance from the capital of the state

$x_5 =$ Crime rate in the city

Step 1: The data provided by the Survey agencies forms the fuzzy soft sets $\Gamma A_1, \Gamma A_2, \Gamma A_3$ over U as follows:

ΓA_1	x1	x2	x3	x4	x5
c ₁	0.8	0.6	0.4	0.6	0.4
c ₂	0.7	0.6	0.4	0.6	0.7
c ₃	0.6	0.5	0.4	0.6	0.5
c ₄	0.9	0.6	0.3	0.9	0.5

ΓA_2	x1	x2	x3	x4	x5
c ₁	0.6	0.5	0.2	0.8	0.5
c ₂	0.6	0.5	0.5	0.4	0.6
c ₃	0.4	0.6	0.4	0.5	0.7
c ₄	0.8	0.4	0.2	0.7	0.5

ΓA_3	x1	x2	x3	x4	x5
c ₁	0.7	0.4	0.3	0.7	0.6
c ₂	0.5	0.7	0.3	0.5	0.5
c ₃	0.5	0.7	0.4	0.4	0.6
c ₄	0.7	0.5	0.4	0.8	0.5

So taking the average of the above three soft sets $\Gamma A_1, \Gamma A_2, \Gamma A_3$ we get the performance fs-set ΓA over U .

Step 2.: Construct an fs-set ΓA over U as given in the following table

ΓA	x1	x2	x3	x4	x5
c_1	0.7	0.5	0.3	0.7	0.5
c_2	0.6	0.6	0.4	0.5	0.6
c_3	0.5	0.6	0.4	0.5	0.6
c_4	0.8	0.5	0.3	0.8	0.5

Then $[a_{ij}]_{m \times n}$ is called an $m \times n$ fs-matrix of fs-set ΓA over U as given below.

$$[a_{ij}]_{m \times n} = \begin{bmatrix} 0.7 & 0.5 & 0.3 & 0.7 & 0.5 \\ 0.6 & 0.6 & 0.4 & 0.5 & 0.6 \\ 0.5 & 0.6 & 0.4 & 0.5 & 0.6 \\ 0.8 & 0.5 & 0.3 & 0.8 & 0.5 \end{bmatrix}$$

Step 3: Here we have applied Fuzzy soft Relation Operator for the study of different cities in the state for making right decision for establishing the new office in a best suitable city taking their desired parameters.

1. So selection of a city based on parameters

$x_1 =$ Population of the city

And $x_3 =$, Available skilled man power in the city

$$(R_1, C_1) = \{c_1/0.21, c_2/0.24, c_3/0.20, c_4/0.24\}$$

Here two cities c_2 and c_4 get equal largest membership grade so company can opt for either of the city.

2. So selection of a city based on parameters

x_1 = Population of the city

x_3 = Available skilled man power in the city

and x_5 = Crime rate in the city we get

$$(R_2, C_2) = \{c_1/0.105, c_2/0.144, c_3/0.120, C_4/0.120\}$$

Here city c_2 get largest membership grade i.e. 0.144 so city c_2 is the best suitable based on these three parameters.

3. So selection of a city based on parameters x_2 = Distance from Airport & Railway Station

And x_4 =, Distance from the capital of the state

$$(R_3, C_3) = \{c_1/0.35, c_2/0.30, c_3/0.30, C_4/0.40\}$$

Here city c_4 get largest membership grade i.e. 0.40 so city c_4 is the best suitable based on these two parameters.

4. Now selection of the city based on all the five parameters

x_1 = Population of the city

x_2 = Distance from Airport & Railway Station

x_3 =, Available skilled man power in the city

x_4 =, Distance from the capital of the state

x_5 = Crime rate in the city

$$(R_4, C_4) = \{c_1/0.03675, c_2/0.0432, c_3/0.0360, C_4/0.0480\}$$

here, the city c_4 has the largest membership grade (0.0480) based on all five parameters taking together.

7. CONCLUSION

Here in this paper for using fuzzy soft relation operator, we first explained basic concepts of fuzzy soft set theory and operations. Here we have taken a real life problem for fixing the priority of the city based on selected parameters of our choice. This method is more useful and convenient over to other selection decision method that we can use the parameters as per our limited choice while in other methods, generally we get final result taking all the parameters together[37]. So this fuzzy soft set relation operator method can be extended for different type of classical real life problems in decision making.

REFERENCES

- [1] Zadeh LA. Fuzzy sets. Information and Control. 1965;8:338-353.

- [2] Molodtsov DA. Soft set theory- rst results. *Comput. Math. Appl.* 1999;37:19-31.
- [3] Fatimah F, et al. Probabilistic soft sets and dual probabilistic soft sets in decision-making. *Neural Computing and Applications*, forthcoming.
- [4] Maji PK, Biswas R, Roy AR. Fuzzy soft sets. *J. Fuzzy Math.* 2001;9(3):589-602.
- [5] Molodtsov DA. The description of dependence with the help of soft sets. *J. Comput. Sys. Sc. Int.* 2001;40(6):977-984.
- [6] Molodtsov DA. *The theory of soft sets (in Russian)*, URSS Publishers, Moscow; 2004.
- [7] Molodtsov DA, Yu. Leonov V, Kovkov DV. Soft sets technique and its application. *Nechetkie Sistemi I Myakie Vychisleniya.* 2006; 1(1):8-39.
- [8] Maji PK, Roy AR, Biswas R. An application of soft sets in a decision making problem. *Comput. Math. Appl.* 2002;44:1077-1083.
- [9] Maji PK, Biswas R, Roy AR. Soft set theory. *Comput. Math. Appl.* 2003;45:555-562.
- [10] Pawlak Z. Rough sets. *Int. J. Comput. Inform. Sci.* 1982;11:341-356.
- [11] Kong Z, Gao L, Wang L. Comment on A fuzzy soft set theoretic approach to decision making problems. *J. Comput. Appl. Math.* 2009;223:540-542.
- [12] Chen D, Tsang ECC, Yeung DS, Wang X. The parameterization reduction of soft sets and its applications. *Comput. Math. Appl.* 2005;49:757-763.
- [13] Zhan J, Alcantud JCR. A survey of parameter reduction of soft sets and corresponding algorithms. *Artificial Intelligence Review*, forthcoming.
- [14] Xiao Z, Li Y, Zhong B, Yang X. Research on synthetically evaluating method for business competitive capacity based on soft set, *Stat. Methods. Med. Res.* 2003;52-54.
- [15] Xiao Z, Chen L, Zhong B, Ye S. Recognition for soft information based on the theory of soft sets. In: J. Chen eds., *Proceedings of ICSSSM-05*, 2. 2005;1104-1106.
- [16] Mushrif MM, Sengupta S, Ray AK. Texture classification using a novel, soft-set theory based classification, *Algorithm. Lecture Notes in Computer Science.* 2006;3851:246-254.
- [17] Pei D, Miao D. From soft sets to information systems, In: X. Hu, Q. Liu, A. Skowron, T. Y. Lin, R. R. Yager, B. Zhang ,eds., "Proceedings of Granular Computing," *IEEE.* 2005;2:617-621.
- [18] Zou Y, Xiao Z. Data analysis approaches of soft sets under incomplete information. *Knowl. Base. Syst.* 2008;21:941-945.
- [19] Kovkov DV, Kolbanov VM, Molodtsov DA. Soft sets theory-based optimization. *J. Comput. Sys. Sc. Int.* 2007;46(6):872-880.

- [20] Majumdar P, Samanta SK. Similarity measure of soft sets. *New. Math. Nat. Comput.* 2008;4(1):1-12.
- [21] Ali MI, Feng F, Liu X, Min WK, Shabir M. On some new operations in soft set theory. *Comput. Math. Appl.* 2009;57:1547-1553.
- [22] Roy AR, Maji PK. A fuzzy soft set theoretic approach to decision making problems. *J. Comput. Appl. Math.* 2007;203:412-418.
- [23] Som T. On the theory of soft sets, soft relation and fuzzy soft relation,” *Proc. of the National Conference on Uncertainty: A Mathematical Approach, UAMA-06, Burdwan.* 2006;1-9.
- [24] Krishna Gogoi, Alok Kr. Dutta, Chandra Chutia. Application of fuzzy soft set in day to day problems. *International J. of Computer Applications.* 2014;85(7):27-31.
- [25] Bhardwaj RK, Tiwari SK, Kailash Chandra Nayak. A study of solving decision making problem using soft set. *IJLTEMAS.* 2015 ;4(9):26-32.
- [26] Alcantud JCR, Rambaud SC, Torrecillas MJM. Valuation fuzzy soft sets: A flexible fuzzy soft set based decision making procedure for the valuation of assets. *Symmetry.* 2017;9(11):253.
- [27] İrkin R, Özgür NY, Taş N. Optimization of lactic acid bacteria viability using fuzzy soft set modeling. *Int. J. Optim. Control, Theor. Appl. (IJOCTA).* 2018;8(2):266-275.
- [28] Kalaichelvi A, Malini PH. Application of fuzzy soft sets to investment decision making problem. *International Journal of Mathematical Sciences and Applications.* 2011;1(3):1583-1586.
- [29] Karaca F, Taş N. Decision making problem for life and non-life insurances. *J. BAUN Inst. Sci. Technol.* 2018;20(1):572-588.
- [30] Özgür NY, Taş N. A note on "application of fuzzy soft sets to investment decision making problem. *J. New Theory.* 2015;7:1-10.
- [31] Taş N, Özgür NY, Demir P. An application of soft set and fuzzy soft set theories to stock management. *Süleyman Demirel University Journal of Natural and Applied Sciences.* 2017;21(2):91-196,
<http://www.sciencepublishinggroup.com/journal/paperinfo?journalid=604&paperId=10038118>.
- [32] Kong Z, Gao L, Wang L, Li S. The normal parameter reduction of soft sets and its algorithm. *Comput. Math. Appl.* 2008;56:3029-3037.
- [33] Cagman N, Enginoglu S. Soft set theory and uni-int decision making. *Eur. J. Oper. Res.* 2010;207:848-855.
- [34] Cagman N, Enginoglu S. Soft matrix theory and its decision making. *Comput. Math. Appl.* 2010;59(10):3308-3314.
- [35] Cagman N, Tak FC, Enginoglu S. Fuzzy parameterized fuzzy soft set theory and

- its applications. Turk. J. Fuzzy Syst. 2010;1(1):21-35.
- [36] Das P K, Borgohain R. An application of Fuzzy Soft Set in Multicriteria Decision Making Problem. Int. J.of Computer Applications,2012;38(12):33-37.
- [37] Rajesh Kumar Pal Application of Average fs-Aggregate Algorithm for multi-criteria decision making in Real life Problem, AJPAS, 2018;2(2):1-11.